

Trajectory Modelling Techniques Useful to Epidemiological Research

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Trajectory Modelling Techniques Useful to Epidemiological Research: A Comparative Narrative Review of Approaches

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01

Why Model Trajectories?

Why Model Trajectories?

Oversimplification of Data

In many studies, measured health outcomes are **averaged** out and their evolution across the entire study sample or pre-specified observed subgroups is analyzed.

describing populations of individuals using averaged estimates amounts to oversimplifying the complex **intra-** and **inter-individual** variability of the real-life clinical context.

Importance of Subgroups

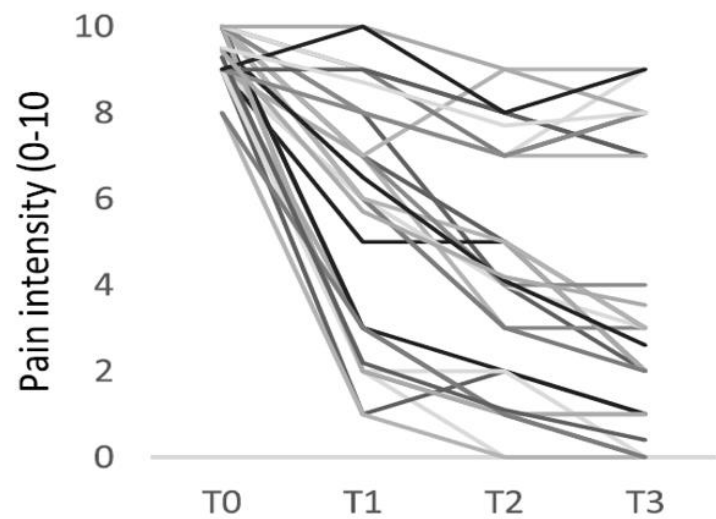
However, in most cases, unknown or unexpected subgroups of individuals share **similar** patterns of clinical symptoms, behaviours, or healthcare utilization.

Need for Precision

Such approaches focus on the relationships among individuals; their purpose is to classify individuals into distinct **subgroups** or classes based on **personal response patterns**.

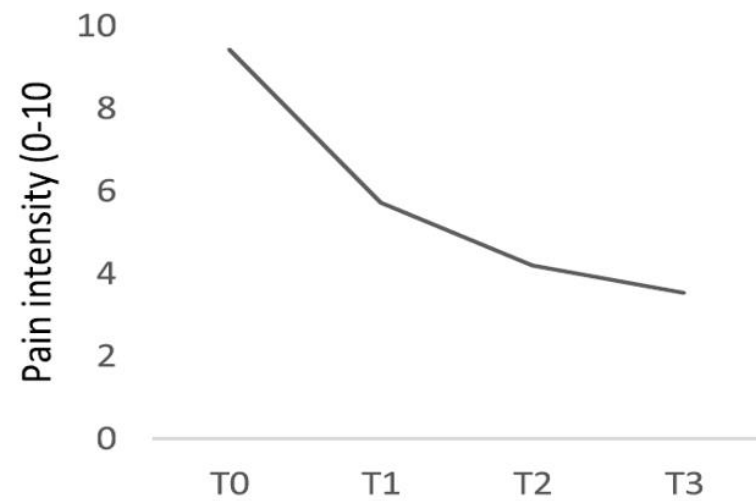
Classification is done so that individuals within a given subgroup share greater **similarities** than individuals from **separate subgroups**.

Individuals progression

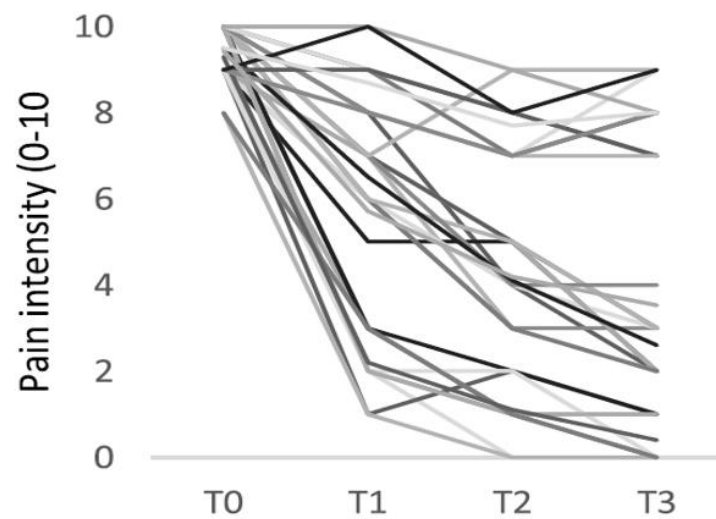


Population average models

Mean score at each time point

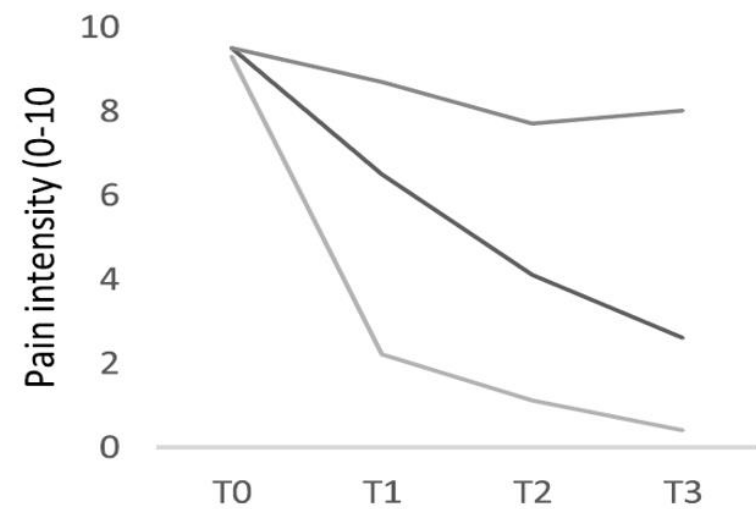


Individuals progression



Trajectory modelling approaches

Trajectories membership



Advantages of using trajectory modeling compared to measures based on sample means:

01

Allows the researcher to better characterize and understand intra- and inter-individual variability and patterns of health outcomes **over time**.

Such approaches can provide scientific evidence to optimize personalized healthcare focused on the needs of **specific** subpopulations.

02

It is useful in exploring **heterogeneity** of health profiles, to identify **vulnerable populations** who require better healthcare, and to identify trajectories leading to the **best health outcomes**.



02

Latent Class Framework

Latent Class Modelling Approaches:

Latent Classes

Latent class modelling are statistical models which include random variables that cannot be directly observed. Individuals are assigned to latent trajectory subgroups on the basis of their **observed** symptoms or behaviours.

Each subgroup is composed of individuals with relatively similar **observations/scores** on observed behaviours.

Temporal Patterns

Rather than evaluating individual time points or change between adjacent time points, longitudinal latent class modelling approaches identify subgroups of subjects who have a **similar** outcome pattern over the study period as a whole.

Four Latent Class Trajectory

Classification Based on Data Type:

longitudinal data:

- ✓ **GMM** (Growth Mixture Modelling)
- ✓ **GBTM** (Group-Based Trajectory Modelling)
- ✓ **LTA** (Latent Transition Analysis)

sectional data:

- ✓ **LCA** (Latent Class Analysis)



03

Growth Mixture Modelling

Growth Mixture Modelling

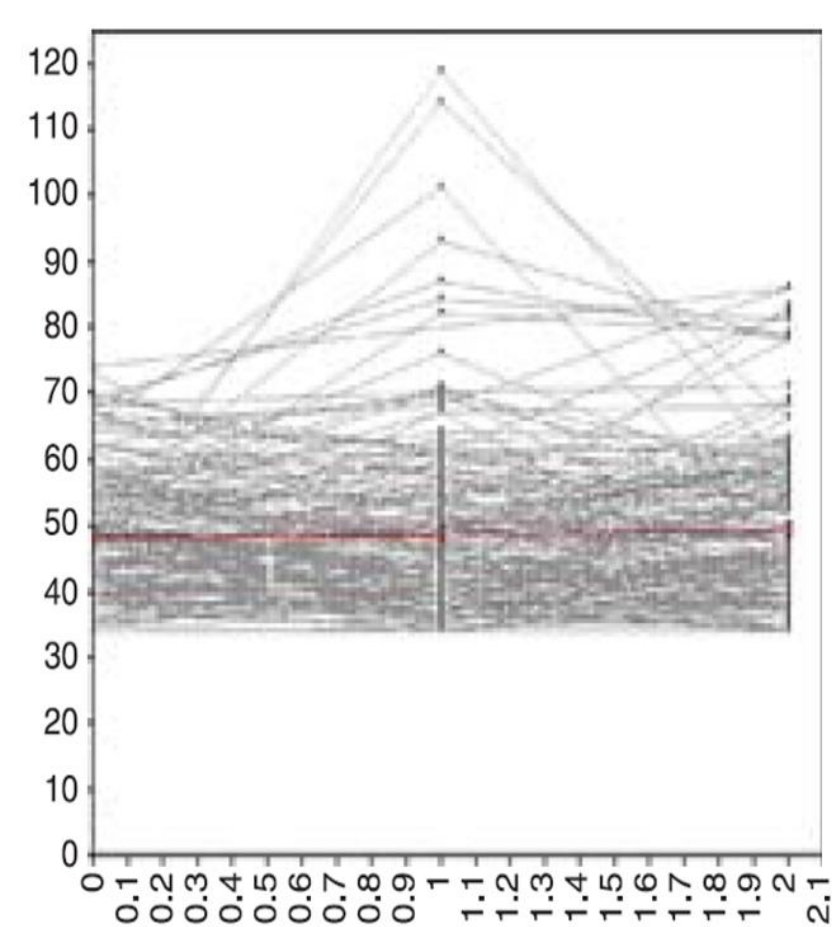
Finite Mixture Model

GMM is a finite **mixture** model. It assumes that in any given population, there exists a **finite** number of unobserved subpopulations or classes (latent classes) with **similar behaviours** or **experiences**.

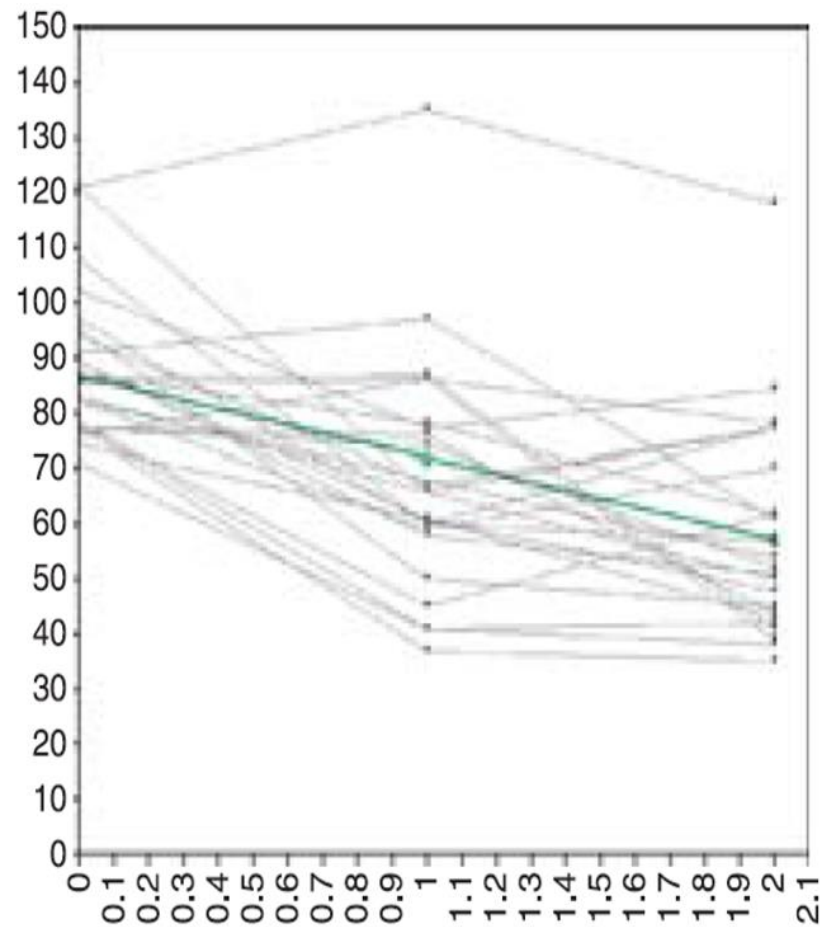
This stands in contrast to classic **statistical models** which assume that all individuals come from the same population with **common population parameters**.

It estimates an average growth curve for each class and allows for variations between **individuals of the same class**. This heterogeneity within classes is captured by introducing **random effects** in the model through which variances of the growth parameters can be estimated (**intercepts** and **slopes**).

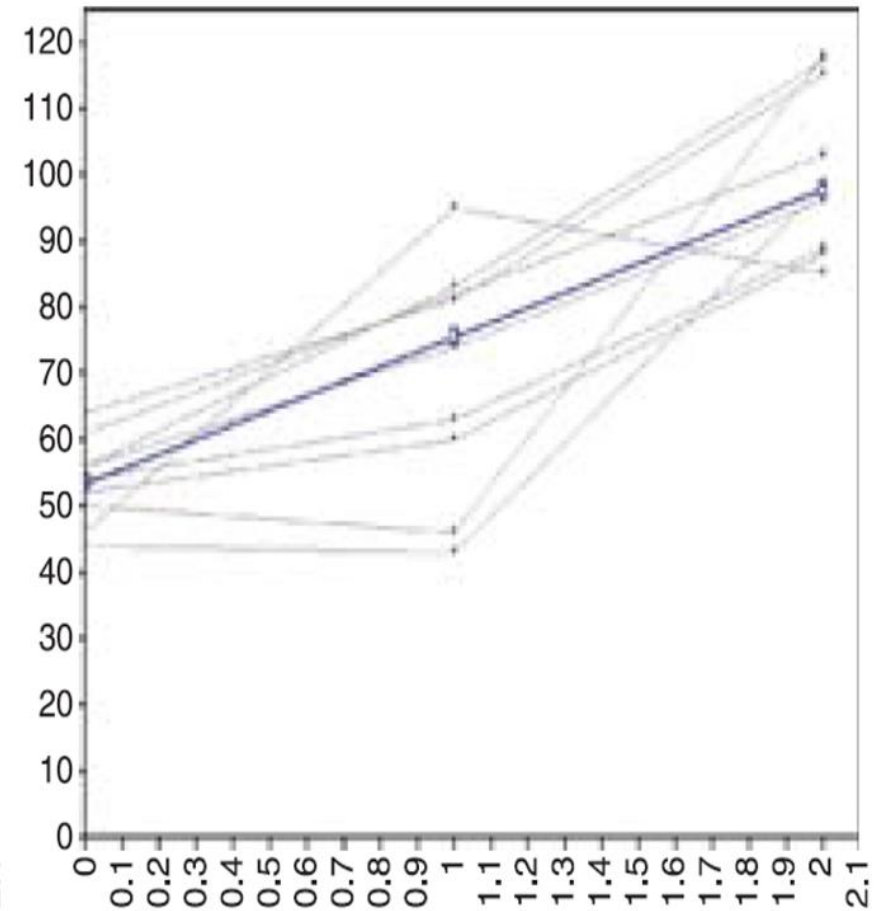
Growth Mixture Modelling



Class 1



Class 2



Class 3

Growth Mixture Modelling

The GMM is a model for **longitudinal** data that has been developed for the study of **continuous** data.

However, it was adapted to handle other types of data such as **count** data (with or without inflation at zero) and **categorical** data.

Four steps for conducting a GMM analysis:

Step 1: Definition of the Problem and Specification of the Number of trajectory Subgroups

The link between the research area and the method is **formalized**.

An appropriate analysis plan is developed. The expected number of **latent classes** and the shape of the curve for each class are hypothesized based on the researchers knowledge of the field and a descriptive analysis of the raw data.

Step 2: Model Specification

- ❑ During this step, a set of models can be specified and estimated. Researchers may make decisions about **growth parameters** (**intercept, slope variance, and covariance**) and the addition of covariates. Substantive theory and previous research should be used to guide these decisions, as much as possible.
- ❑ During these steps, researchers should decide if the **shape** of each trajectory over time should be **linear, quadratic** or **cubic** (intercept and slope parameters).
- ❑ They should also decide if growth factor **variances** should be specific to each class, if **within-class growth factor covariances should be different from zero**, and if outcome residual variances should be invariant with respect to class.

Step 3: Model Estimation

GMM can be estimated by **maximum likelihood** or by **Bayesian methods**.

Step 4: Model Selection and Interpretation

The objective of this step is to determine which of the models tested provides the best or **most reasonable**.

The goodness of fit of the various models should be compared using the **Lo- Mendell-Rubin** adjusted likelihood ratio test

and/or the parametric **bootstrapped** likelihood ratio test ($p < 0.05$ indicates better fit)

and/or the **Bayesian** Information Criteria (BIC) (best models have smaller BIC).

Researchers should also take into account convergence, the ability of the model to provide well separated classes (**entropy near 1.0**), the proportion of the sample in each trajectory (more **than 5% is recommended**), average posterior probabilities (near 1.0), parsimony and the usefulness of the observed latent classes in practice.

Lo- Mendell-Rubin adjusted

	2-class vs 3-class	3-class vs 4-class	4-class vs 5-class
Value	1088.997***	392.121**	204.070
P value	0.000	0.001	0.051

*p<.05, **p<.01, ***p<.001.

Growth Mixture Modelling

Advantages

- ✓ -Handling missing data
- ✓ -Allowing for correlated residuals
- ✓ -Latent class modelling
- ✓ -Estimates a mean growth curve
- ✓ -Identification of individual heterogeneity

- ✓ -Complexity of interpreting results

Limitations



04

Group-Based Trajectories Modelling

Group-Based Trajectories Modelling

Like GMM, GBTM—also known as Latent Class Growth Analysis (LCGA)—is a finite **mixture** model.

While GMM estimates the withinclass variance, GBTM assumes that there is **no variation between individuals in the same class** (no within-class variance on the growth factors). Indeed, GBTM is a **simplified** version of GMM.

Group-Based Trajectories Modelling

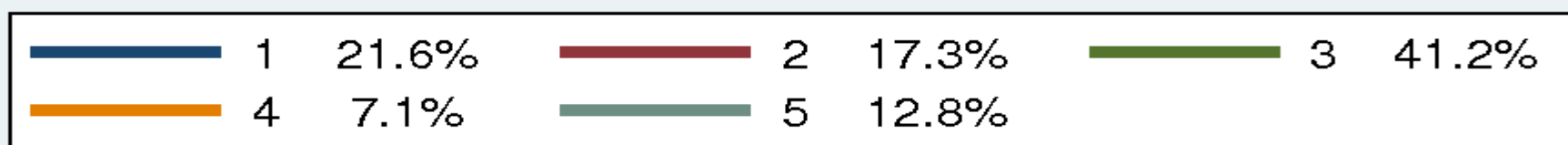
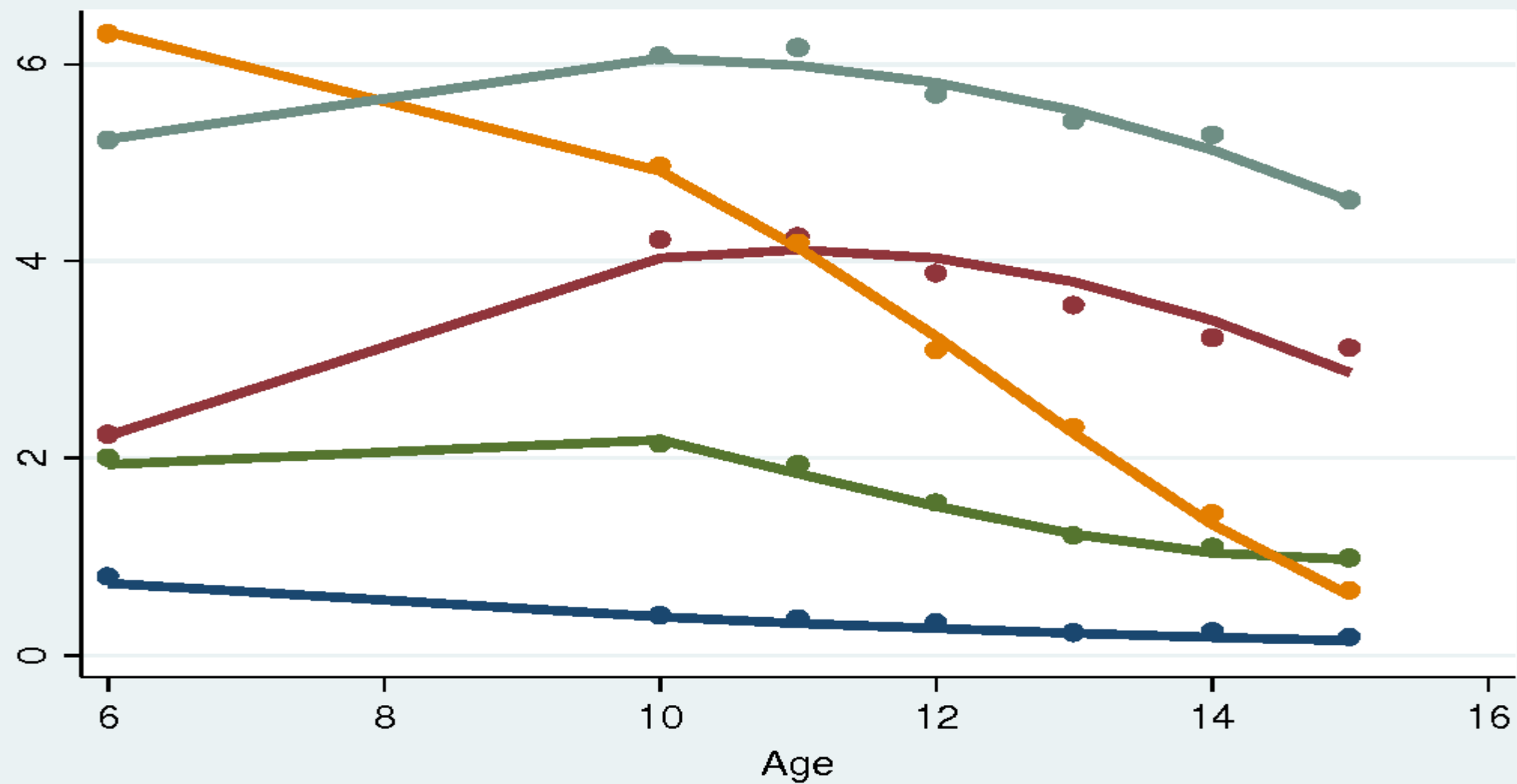
For example, in the case of the aforementioned three pain intensity trajectory subgroups (no improvement, gradual improvement, rapid improvement), GBTM assumes that in each class, individuals have the same pain intensity evolution. The proportion of the population belonging to each of these subgroups is then estimated.



The model also determines, for each individual, the probability of belonging to one subgroup or another (posterior group probability).



As in GMM, Parameters are estimated by maximizing likelihood. Covariates (that vary or not over time) can also be included in the model.



Four steps for conducting a GBTM analysis:

Step 1: Definition of the Problem and Specification of the Number of Trajectory Subgroups.

Same as previously described for GMM.

Step 2: Model Specification

- ❑ It is suggested to **first test a one-group** model, then gradually adjust the maximum logical number of subgroups.
- ❑ This maximum logical number of **subgroups should be greater than the expected number** of subgroups.
- ❑ If the quadratic component of this model is **not significant, the model for a linear trajectory** is to be run to determine the BIC value of this model.
- ❑ If the **quadratic component** of the model for a trajectory is significant, the analysis of the quadratic model for two trajectories is performed

Step 3: Model Estimation

Same as previously described for GMM.

Step 4: Model Selection and Interpretation

- 1) preference for a **useful** and parsimonious model that fits the data well
- 2) close correspondence between the estimated probability of each subgroup and the proportion of individuals classified in such subgroup according to the rule of attribution of the **maximum probability** of belonging
- 3) average **posterior probabilities** of subgroup membership greater than or **equal to 0.7** for each subgroup
- 4) sufficient number of individuals in each subgroup (**more than 5%**)
- 5) reasonably **narrow confidence intervals**
- 6) difference of **BICs** between two models with different numbers of trajectory subgroups

Group-Based Trajectories Modelling

Advantages

GBTM is a simpler specification of the GMM, and both have the same advantages regarding handling missing data and allowing for correlated residuals.

Unlike GMM, GBTM estimates **fewer parameters** and can thus run faster with fewer errors.

GBTM supposes that all individuals in a trajectory class have the same behaviour, whereas GMM allows for within-class variation). This means that, when GBTM is used, researchers can discuss differences between subgroups, but not differences within Subgroups(.

Limitations



05

Latent Transition Analysis

Latent Transition Analysis (LTA):

The model assumes that individuals can **change** their **class membership over time**.

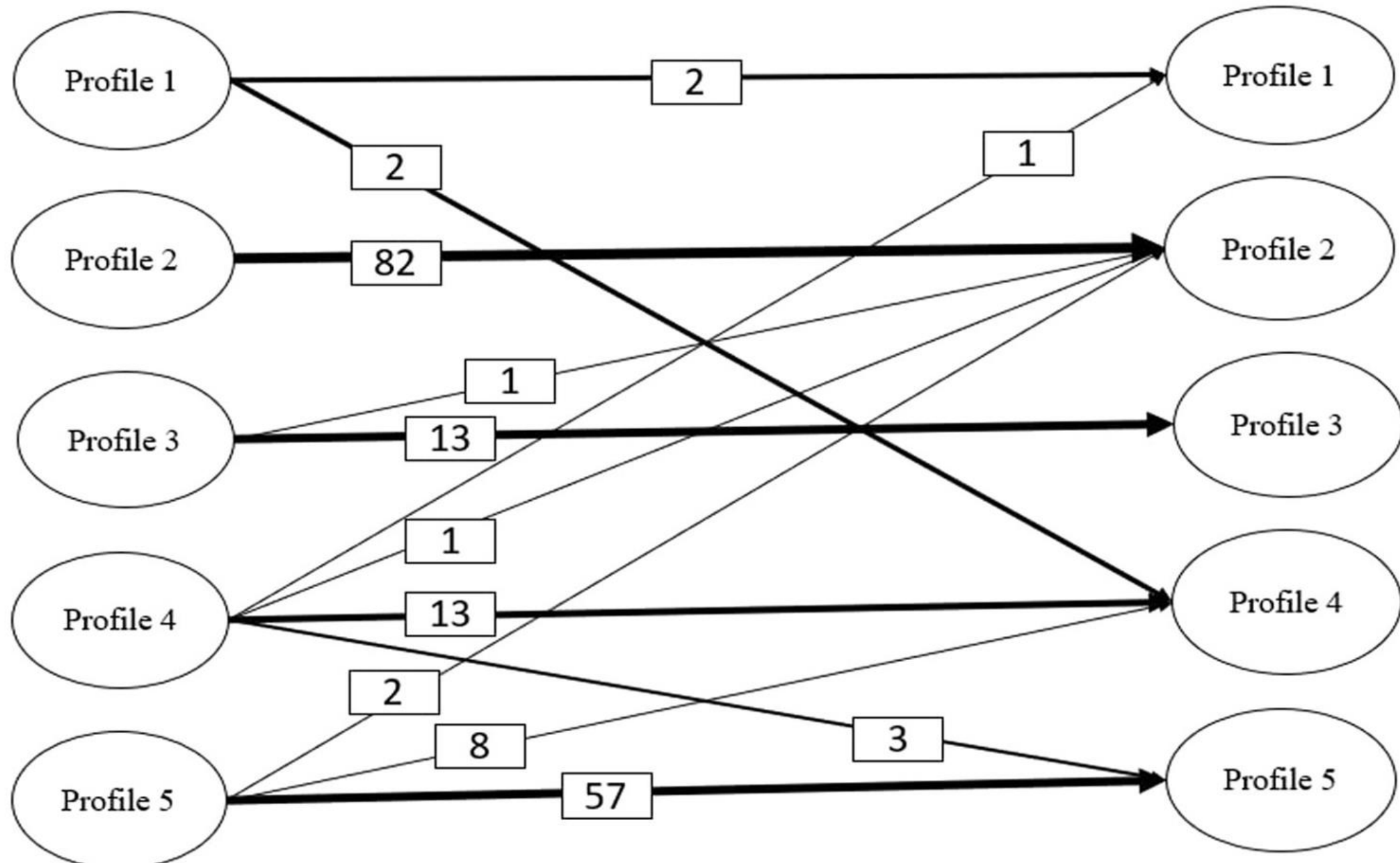
For example, in the case of three pain intensity subgroups (mild/moderate/severe), LTA allows for individuals to switch from the severe subgroup at one time point to the mild or moderate subgroup at the next time point, and so on.

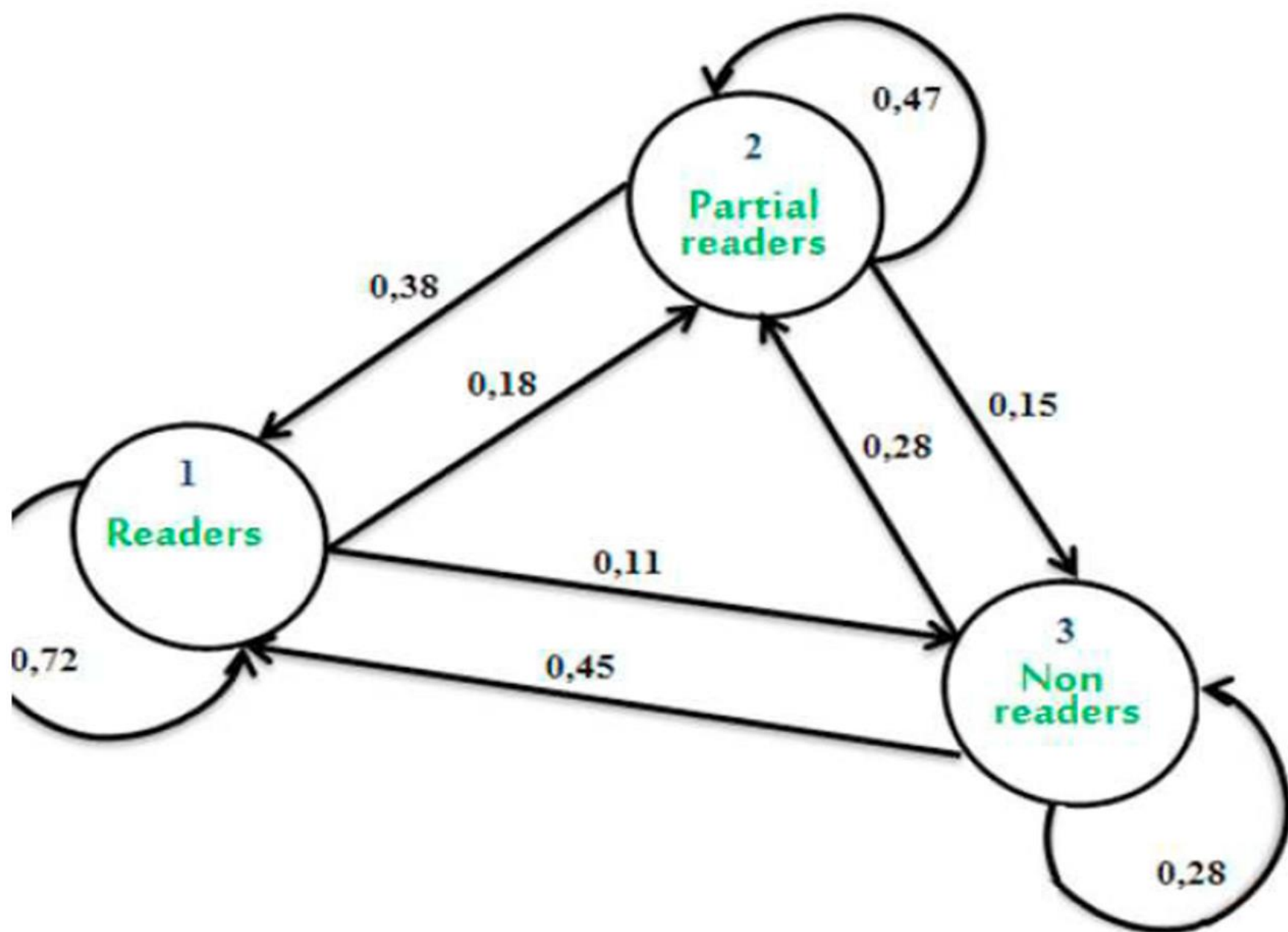
LTA is used to analyze changes in multiple categorical variables **over time** (eg, yes/no, mild/moderate/severe).

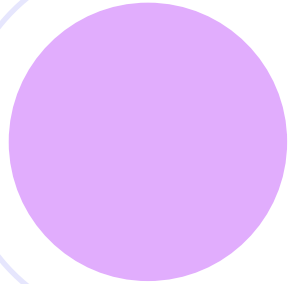
LTA uses observed data from a set of **categorical** variables to define a latent variable for each time point.

Time 1

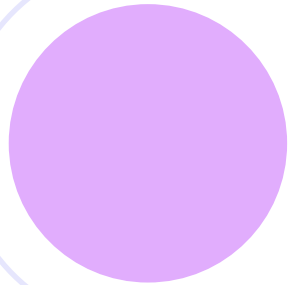
Time 2







The primary objective of this approach is to study the probability of transition of an individual from one class at one time point to another class at the next time point.



Like GMM and GBTM, covariates can be added to LTA models. However, LTA requires that the number of classes be chosen before adding covariates principally to avoid a potential change in class number with and without covariates.

The model estimates the following parameters:

1

The latent status membership probabilities at Time 1

2

The proportion of the population in each latent class at each time point (latent status has been defined as a subgroup/class in which individuals' memberships can change over time)

3

The conditional probabilities of making a transition from one latent status to another over time (eg, probability of being in latent status L2 at Time t given a latent status L1 at Time t-1)

4

The item-response probabilities conditional on latent status membership (analogous to posterior group probabilities).

Four steps for conducting a LTA analysis:

Step 1: Definition of the Problem and Specification of the Number of trajectory Subgroups.

The choice of the number of latent classes is based on the result of a hypothesis test.

Step 2: Model Specification

During this step, researchers make a decision about the time invariance of item-response probabilities, the measurement invariance for transition probabilities (in order to achieve model identification and to facilitate the interpretation of classes prevalence), and the addition of covariates.

Step 3: Model Estimation

During this step, the estimation method should be chosen before fitting the models. LTA models can be estimated by **maximum likelihood** using the expectation maximization algorithm.

They can also be estimated with **Bayesian methods** using Markov chain Monte Carlo algorithms.

Step 4: Model Selection and Interpretation

In the LTA, the AIC and BIC are used to select the best model, favoring the one for which these two values are smaller in absolute value.

Advantages

- Comparing different subgroups
- Useful to model a change over time

- Large sample sizes
- Number of time points

Limitations

THANK YOU